DETERMINANTS OF ENVIRONMENTAL HEALTH RELATED DISEASES IN KENYA WITH GENERALIZED LINEAR MIXED MODELS: ANALYSIS OF KENYA INTEGRATED HOUSEHOLD BUDGET SURVEY

BY

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DECLARATION

This research project is my original work and has not been submitted for examination in any other university.

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This research paper has been submitted for examination with our approval as university supervisors.

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DEDICATION

I dedicate this degree to my husband Joseph Kirago, and my father John Muraya for their outstanding support, prayers, encouragement and nurturing conducive environment during my study period.

Contents

LIST OF ABBREVIATIONS

GLMEM	Generalized Linear Mixed effects Model
GLMM	Generalized Linear Mixed Model
GLMs	Generalized Linear Models
ML	Maximum Likelihood
REML	Restricted Maximum Likelihood
PQL	Penalized quasi Likelihood
MQL	Marginal Quasi Likelihood
N-A	Nelson Aalen (Estimation)
DHS	Demographic and Health surveys
DIC	Deviance Information Criteria
PSUs	Primary Sampling Units
AIC	Akaike Information Criteria
KIHBS	Kenya Integrated Household Budget Surveys

ABSTRACT

Generalized linear models (GLMs) form a class of fixed effects regression models for several types of dependent variable, whether continuous, dichotomous or counts.

Common GLMs include linear regression, Logistic regression and Poison regression. These models have typically been used a lot in modeling of data arising from a heterogeneous population under the assumption of independence. However, in applied science and in real life situations in general, one is confronted with collection of correlated data (Mark Aerts et al, 2005). This generic term embraces a multitude of data structures, such as multivariate observations, clustered data, repeated measurements, longitudinal data, and spatially correlated data. Generalized Linear Mixed Models (GLMMs), also called Generalized Linear Mixed Effects Models (GLMEMs) are able to handle extra ordinary range of complications in regression- type analyses. They are often used to handle correlations as it arises in longitudinal and other clustered data.

In this paper we describe use of GLMMs to explain different factors and their influence on an individual morbidity in Kenya. We use maximum likelihood (ML) as the main estimation method. We also use Restricted Maximum Likelihood (REML) estimation when we relax the assumption of equal cluster sizes, to help in estimating intra and inter block weights. We shall assume normality of the random effects.

The (2005/6) Kenya Integrated Household Budget Survey findings pointed out that there has been a worsening health situation in Kenya. The result further outlined that the number of individuals having environmental health related disease had increases as compared to the previous studies. The higher prevalence of individual morbidity was associated with social,

economic and demographic factors. Reducing environmental health related diseases to a population remains one of the thorny issues that face developing countries, among them Kenya. Therefore, there is an urgent need to explain the way forward in addressing and guiding policy towards this noble goal. In our results, we deduced that gender increases the log-odds of a individual getting a disease, while people who are living in good housing conditions reduce the log-odds of individual experiencing morbidity. Main source of drinking water was also significant in explaining individual morbidity in Kenya. The human waste disposal method was also significant in explaining morbidity among individuals. This study can however be extended to incorporate income level of individuals. Individuals with low level of income are believed to be more likely to experience environmental health related diseases than individuals with higher levels of income.

CHAPTER ONE

BACKGROUND

Generalized linear mixed models (GLMMs) continue to grow in popularity due to their ability to directly acknowledge multiple levels of dependency and model different data type. GLMMs extend the generalized linear model, as proposed by Nelder and Wedderburn (1972) and comprehensively described in McCullagh and Nelder (1989), by adding normally distributed random effects on the linear predictor scale in order to include the concept of correlated data such as clustered data.

GLMM is one of the most useful structures in modern statistics, allowing many complications to be handled within the familiar linear model framework. The fitting of such models has been the subject of a great deal of research over the past decade. Early contributions to fitting various forms of the GLMM include Stiratelli, Laird and Ware (1984), Anderson and Aitkin (1985), Gilmour, Anderson and Rae (1985), Schall (1991), and Breslow and Clayton (1993).

Most literature on GLMM is around grouped data. For any model, parameter estimation is always one of the most important aspects of statistical inference. Many researchers have made efforts to estimate parameters using GLMMs. For instance, Hall; Hall, (2000) applied Maximum Likelihood (ML) estimation and Yau and Lee, (2001) applied hierarchical likelihood method of estimation to zero-inflated (ZI) mixed models. In this project, ML for normal random effect of GLMMs and Restricted maximum likelihood (REML) method when assuming random effect distribution is unknown will be used.

This study seeks to fit generalized linear mixed effects model to household data that was collected in 2005/6. In this survey, clusters were randomly selected across all the districts in Kenya. In each selected cluster, households were randomly selected with equal probability in each cluster; members in the selected households were interviewed. I therefore propose that cluster variable to introduce the random effect in this data. It is assumed that members in the same cluster are more likely to experience similar morbidity structures compared to members in different clusters.

1.2 Problem statement

Efforts to understand and predict determinants of environmental health related diseases in Kenya have been a big challenge. However, there has been lots of suggestion that all causes of morbidity are a result of socioeconomic factors such as income and poverty. These variables are normally collected based on multistage clustered sampling scheme. A normal regression model may not be able to capture the possible inter-class correlation in the data. In this paper, I propose to account for the interclass correlation in morbidity data, while identifying all the factors that are highly associated with environmental health related diseases.

1.3 Study Objectives

1.3.1 Main Objective

This study seeks to define factors that are associated with the probability of an individual in a population experiencing an environmental health related disease in Kenya using Kenya Integrated Household Budget Survey.

1.3.2 Specific objectives

The specific objectives of the study are:

1. Develop a statistical model that defines the factors that explain environmental health related morbidity in Kenya, while accounting for inter-class correlation in the data.
2. To measure the effects of household variables on environmental health related diseases

1.4 Significance of the study

Environmental health related morbidity continues to be an issue for most demographers with no clear model that can be used to explain causes of morbidity in Kenya. Previous studies have sought to model cause –specific morbidity without accounting for inter-class correlation in the data. Also, many of the direct determinants of morbidity are linked to environmental and household characteristics. This leaves us with a feeling that morbidity is not only correlated between households closer together than households further apart. This paper therefore develops a model that shall predict the probabilities of having environmental health related disease while accounting for random effects in the data.

CHAPTER TWO

LITERATURE REVIEW

Generalized linear mixed effects models have been used for long time and more so by epidemiologists in the analysis of dichotomous data. Most of the recent contributions to the use of GLMMs was a study by Kandala, Nyovani, (2004). Their study aimed at describing the spatial variation in the prevalence of diarrhea, cough and fever among children under 5 years using the 1992 Demographic and Health surveys (DHS) of Malawi and Zambia. Individual data record was constructed for 3660 children in Malawi and 5268 children in Zambia. Each record represents a child and consists of morbidity information and a list of covariates.

Geo-additive logistic analyzes was used on the probability of a child being ill with malaria, cough, and diarrhea during the preference period to determine the socio-economic, demographic variables that are associated with these three ailments while simultaneously controlling for spatial dependence in the data and possibly nonlinear effects of covariates.

The response variable applied was defined as

y_{it} = { 1: if a child i was ill during the preference period t

0: if a child i survive the illness,

Two models were fit in this data: simpler parametric probit model and probit model with dynamic and spatial effects for the probability of falling ill at month t.

M1: $n_{it}=X'_{it}B$.....(2.1)

M2: $n_{it}=f_1(\text{age}) + f_2(\text{mab}) + f_{unstr}(\text{dist}) + f_{str}(\text{dist}) + X'_{it}B$.....(2.2)

The fixed effects in model M1 included all the covariates with constant fixed effects. When the two models were compared, it turned out that model M2 was superior in terms of Deviance Information Criteria (DIC) [Spiegelhalter et.al., 2002] which is a method used for model comparison. In addition, model M2 in the DIC, accounted for the unobserved heterogeneity that might exist in the data, which cannot be captured by the covariates.

The effects of f_1 and f_2 were modeled by cubic penalized splines with second order random walk penalty. Spatial affects f_{str} (s) were experimented with different prior assumptions.

In both countries models were estimated where either a structured or an unstructured effect was included as well as a model where both effects were included. As a result there was clear evidence for both countries of spatial correlation among neighboring districts. Hence, a spatially correlated effect f_{str} was included into the predictors of the final models. Additionally, an unstructured effect f_{unstr} was included because there was evidence of local extra variation in the highly urbanized areas in Malawi and Zambia.

Including the spatial component $f_{unstr} + f_{str}$ (dist) increases model complexity. With such model, it is assumed that random components at the contextual level (district) are mutually independent. The estimates of the presumed spatial correlated districts level random effects showed strong evidence of spatial dependence.

Hedeker and Gibbons (2003) described a random effects ordinal probit regression model, examining longitudinal data collected in the NIMH Schizophrenia Collaborative Study on treatment related changes in overall severity. The dependent variable was item 79 of the Inpatient Multidimensional Psychiatric Scale (IMPS; [30]), scored as: (a) normal or borderline mentally ill, (b) mildly or moderately ill, (c) markedly ill, and (d) severely or among the most

extremely ill. In this study, patients were randomly assigned to receive one of four medications: placebo, chlorpromazine, fluphenazine, or thioridazine.

Here, a logistic GLMM with random intercept and trend was fit to these data using SAS PROC NLMIXED with adaptive quadrature. Fixed effects included a dummy-coded drug effect placebo = 0 and drug = 1), a time effect (square root of week; this was used to linearize the relationship between the cumulative logits and week) and a drug by time interaction.

The results indicated that the treatment groups do not significantly differ at baseline (drug effect), the placebo group does improve over time (significant negative time effect), and the drug group has greater improvement over time relative to the placebo group (significant negative drug by time interaction). Thus, the analysis supports use of the drug, relative to placebo, in the treatment of schizophrenia. Comparing this model to a simpler random intercepts model yields clear evidence of significant variation in both the individual intercept and time-trends likelihood-ratio.

Also, a moderate negative association between the intercept and linear time terms is indicated, expressed as a correlation it equals -.40, suggesting that those patients with the highest initial severity show the greatest improvement across time (e.g., largest negative time trends). This latter finding could be a result of a floor effect', in that patient with low initial severity scores cannot exhibit large negative time-trends due to the limited range in the ordinal outcome variable.

There were more work on morbidity and factors associated to morbidity that involved GLMM that was done in (2002) by Narayan, Sarah B. et al, (2002). This analysis sought to examine trends and differentials in diarrhea prevalence and treatment in Brazil between 1986 and 1996 using data from Demographic and Health Survey program. Information on child health, health-related behavior, use of health care services and several other topics was collected. The survey was based on a multistage clustered sampling scheme. A total of 8,369 dwellings units was selected for the survey across 337 primary sampling units (PSUs) whereby PSUs represented the entire country. Interviews were completed with 5,892 women aged 15 to 44 years and information on diarrhea was obtained for 3,183 children born to these women.

Multilevel logistic regression was used to model the relationship between the diarrhea prevalence and the background and intermediate factors. The dependent variable was a binary response, y_{ijk}, that indicated whether the i^{th} child of the j^{th} family living in the k^{th} community had diarrhea (y_{ijk}= 1) or not (y_{ijk} =0). The probability of a child having diarrhea was defined as p_{ijk} = pr (y_{ijk}=1) and logit transformation of p_{ijk} modeled as a linear function of the covariates in the model:

$$\text{Log}\,[p_{ijk} / (1-p_{ijk})] = X'_{ijk}\beta_1 + X'_{jk}\beta_2 + X'_k\beta_3 + u_{jk} + v_k \quad \text{..... (2.3)}$$

u_{jk} represents a family-level random effect and v_k a community-level random effect that are each normally distributed with a zero mean and variance δ_u^2 and δ_v^2 respectively. X_{ijk} represents background child covariates, X_{jk} family covariates and X_k community covariates.

Model 2.4 included intermediate child covariates (W_{ijk}) and intermediate family covariates (W_{jk}).

$$\text{Log}\,[p_{ijk} / (1-P_{ijk})] = W'_{ijk}\gamma_1 + W'_{jk}\gamma_2 + X'_{ijk}\beta_1 + X'_{jk}\beta_2 + X'_k\beta_3 + u_{jk} + v_k \quad \text{.....(2.4)}$$

Model 2.3 and model 2.4 allowed them study how background factors directly and indirectly affected diarrhea prevalence. Model 2.3 showed the total effect of each background factor on diarrhea prevalence.

This study showed that the family and the community random effects were statistically significant in mode; 2.3 and model 2.4, although unobserved family effects were far more important than unobserved community effects. The variance of the family random effect (2.33) was more than six times as large as the variance for the cluster random effect (0.35). The intra-family level correlation was .45 while the intra-cluster correlation was only .06.

The large family-level variance indicates that there was a strong correlation in the chances of siblings having diarrhea that may be the result of important unmeasured maternal characteristics and household environmental factors (Sastry, 1997).

The study also found that there were significant effects on diarrhea of child age, mother's education, father's education, parent's marital status, rural-urban place of residence, and region of residence.

More work to the use of GLMMs was a study by Gruder, Gruder et AL, (1993). This study aimed at describing smoking cessation, whereby 489 individuals were randomized into three groups; Control, discussion, or social support conditions. The control group was given a self help manual and encouraged to watch 20 twenty television programs on smoking cessation. Subjects on the experimental groups were in addition given a chance to participate in group meetings and were given further training in support and relapse prevention. To analyze the data as binary response variables, the two experimental groups were combined together into one category

called experimental group. Data were collected at four telephone interviews: post intervention, and 6, 12, and 24 months later. Smoking abstinence rates at these four times were as follows:

-Control group: = 109, 97, 92, and 77

-Experimental group: = 380, 357, 337, and 295

Two logistic GLMM were fit to this data i.e. a random intercept model and a random intercept and linear trend of time model. In this study, the analysis was based on the probability of smoking abstinence and not the probability of smoking. The fixed effect were the group, with 0=control and 1=experimental. Based on a likelihood-ratio test, the random intercept and linear trend of time model was preferred (with a –2loglikelihood ratio=1594.7) to the random intercept model (with a -2loglikelihood ratio=1631.0). As a result, there was a clear evidence of subjects varying by both the intercepts and the time trends. Both models had a nonsingular time effect, but the treatment was highly significant. Interaction between condition and time was non-significant in the both models, which suggested a declining condition over time. The interaction was non-significant in the random intercepts and time trend model, but was significant in the random intercept model.

This study showed that the significance of model terms can highly depend on the structure of the random effects. Therefore, a researcher must decide upon a reasonable model for the random effects as well as for fixed effects. A recommended approach is to perform a sequential model selection procedure such as step wise regression analysis. Here one includes all the possible covariates of interest into the model and selects between the possible models of random effects using model fit criteria such as the likelihood ratio test, Deviance analysis, Akaike Information Criteria among others. In this study, I shall take advantage of the superiority of Akaike

Information Criteria of being adjusted for both the sample size and the number of parameters in the model. For model selection criterion, I shall use the backward stepwise selection, whereby the model with a smaller AIC value being preferred to the model with larger value.

Carla J. Machado and Ken Hill July (2003) [19] used data for the (1998) –birth cohort, City of S.Paulo, Brazil. The hypothesis was that early infant morbidity may produce adverse outcomes in subsequent life. The duo used Apgar units to estimate early infant morbidities, with a low Apgar score being a convenient measure of early infant morbidity. The study used determinants of early infant morbidity (sex, plurality, mode of delivery, prior losses, gestation age, prenatal care and birth weight, parity and maternal age, race, maternal education and community development).

Information was extracted from 2009,628 birth records, and used multivariate logistic regression to assess the effect of each independent variable on Apgar score less than seven at one minute and Apgar score less than seven at five minutes.

The outcome variable was whether or not an infant had an Apgar score below seven at one minute or not and whether or not an infant had an Apgar score below seven at five minutes. The explanatory variables were classified as;

1. Proximate determinants-birth weight, gestation age, prenatal care, sex, plurality, prior losses and mode of delivery
2. Less proximate determinates- parity and maternal age
3. Distal determinants- race, maternal education and community development

To obtain an adjusted odds ratio, a multivariate logistic regression model was used in order to model the two dichotomous outcomes. Because characteristics of mothers and infants from the same community were related, the standard errors were corrected for lack of independence between observations using the Huber/White Sandwich correction, which assumes that observations are independent across clusters but not within clusters (the community of mother's residence at the time of birth).

From their results, Low birth weight, prematurity and community development had strong prediction of morbidity. Maternal education showed strong negative correlation with both Apgar scores. The negative correlations between maternal schooling and Apgar scores were observed after prenatal care, parity and maternal age were included in the model. Children of very young adolescent mothers had lower Apgar scores at one minute (but not at five minutes) than those born to mothers aged 15 to 19. Parity one or higher was associated with decreased odds of low Apgar scores. Cesarean section and operative delivery were also strongly associated with higher odds of early infant morbidity.

CHAPTER THREE

METHODOLOGY

3.0 Introduction

There are many probability distributions that can be used to model the socio-economic factors affecting environmental health related diseases in households. In this chapter, we describe the data and variables that will be used then examine various models that can be used to model clustered data.

3.1 Data

The data for this study comes from the Kenya Integrated Household Budget Survey (KIHBS) conducted by Kenya National Bureau of Statistics in (2005/6). In KIHBS, data was collected over a period of 12 months, which covered all possible seasons. This survey was to collect a wide spectrum of socio-economic indicators required to measure, monitor and analyze the progress made in improving living standards. The Household Questionnaire was designed to collect information on the following: demographics, housing, education, health, agriculture and livestock, enterprises, expenditure and consumption, among others.

The Survey was conducted in 1,343 randomly selected clusters across all districts in Kenya and comprised 861 rural and 482 urban clusters, 10 households were randomly selected with equal probability in each cluster resulting in a total sample size of 13,430 households. This study is confined to members of the household who experienced any sort of disease at the time of the study. This produces a data set comprising about 66,725 individuals.

3.2 Dependent Variable

The outcome variable of interest (morbidity) asked whether a member of household had suffered from environmental health related disease. This variable is binary in nature with values (1=household member had environmental health related disease, 0= household member had not experienced environmental health related disease).

3.3 Explanatory Variables

This study used explanatory variables available in the Kenya Integrated Household Budget Survey data. These include socioeconomic and demographic variables. The socioeconomic variables used in the study include gender, highest level of education, individual working status, main source of drinking water, housing condition and means of human waste disposal. The demographic variable used is area of residence i.e. rural/urban.

3.4 Modeling

In this section, we review some of the statistical methods and techniques that will be used in herein. It also gives us more on the basic concepts that are used in the build up to use GLMMs in analysis of morbidity data.

3.5 Exponential Distribution Family

The distribution of a random variable y_i (with mean μ_i) is said to belong to the exponential family if it has a probability density function of the form;

$$f(y_i, \theta_i, \Phi) = exp\left[\frac{y_i\theta - b(\theta_i)}{a(\Phi)} + c(y_i, \Phi)\right] \quad (3.1)$$

Φ is a constant dispersion parameter, θi is the natural or canonical parameter that can be expressed as some function of mean μ_i and $k\theta_i$ is a cumulant generating function. Among many of the common

distributions that are known to belong to this distribution include; Normal, Gamma, Poisson and Binomial.

3.6 Generalized Linear Models (GLM's)

The *generalized linear model* (GLM) refers to a larger class of models popularized by McCullagh and Nelder (1982, 2nd edition 1989). In these models, the response variable y_i is assumed to follow an exponential family distribution with mean μ_i, which is assumed to be some (often nonlinear) function of $x^T{}_i\beta$.

They represent a class of fixed effects regression models for several types of dependent variables (i.e. continuous, dichotomous, counts). Thus, it can be said that the generalized linear model involves logistic models for binary dependent variables, log linear analysis, Poisson regression, etc.

There are three components to any GLMs:

1. **Random Component** – refers to the probability distribution of the response variable (Y); e.g. normal distribution for Y in the linear regression, or binomial distribution for Y in the binary logistic regression. Y_i's are independent and random variables with mean $E(Y_i) = \mu_i$ and are member of the exponential family of distributions.
2. **Systematic Component** - specifies the explanatory variables (X_1, X_2, ... X_k) in the model, more specifically their linear combination in creating the so called linear predictor; e.g., $\beta_0 + \beta_1 x_1 + \beta_2 x_2$
3. **Link Function, η or $g(\mu)$** - specifies the link between random and systematic components. It says how the expected value of the response relates to the linear predictor

of explanatory variables; e.g., $\eta = g(E(Yi)) = E(Yi)$ for linear regression, or $\eta = logit(\pi)$ for logistic regression.

Generalized linear models are based on the following assumptions:

- The data $Y_1, Y_2, ..., Y_n$ are independently distributed, i.e., cases are independent.
- The dependent variable Y_i does NOT need to be normally distributed, but it typically assumes a distribution from an exponential family (e.g. binomial, Poisson, multinomial, normal)
- GLM does NOT assume a linear relationship between the dependent variable and the independent variables, but it does assume linear relationship between the transformed response in terms of the link function and the explanatory variables; e.g., for binary logistic regression $logit(\pi) = \beta_0 + \beta X$.
- Independent (explanatory) variables can be even the power terms or some other nonlinear transformations of the original independent variables.
- The homogeneity of variance does NOT need to be satisfied and errors need to be independent but NOT normally distributed.
- It uses maximum likelihood estimation (MLE) rather than ordinary least squares (OLS) to estimate the parameters, and thus relies on large-sample approximations.

3.7 Generalized Linear Mixed Models (GLMMs)

The **generalized linear mixed** model (GLMMs) is an extension to the **generalized linear models** in which the linear predictor contains random effects in addition to the usual fixed effects. They extend the idea of linear mixed models to non-normal data.

The general form of the model (in matrix notation) is:

$$y=X\beta+Z_{\gamma}+\varepsilon \qquad (3.2)$$

Where y is a column vector, the outcome variable; X is a matrix of the p predictor variables; β is a column vector of the fixed-effects regression coefficients (the "betas"); Z is the design matrix for the q random effects (the random complement to the fixed X); γ is a vector of the random effects (the random complement to the fixed β); and ε is a column vector of the residuals, that part of y that is not explained by the model, Xβ+Zγ

The inclusion of random effects in the predictor is to account for over dispersion, correlation and heterogeneity in the data. Since correlation is a natural feature of clustered data as much as in the longitudinal data, GLMMs have been used extensively for such data Aitkin, (1996), Stiratelli et al, (1984); Zeger et al, (1988).

GLMMs for a cluster data are defined as follows:

Suppose that the observations on the i^{th} cluster consists of response y_{ij}, covariates x_{ij} and z_{ij} associated with the fixed and random effects respectively, for i=1,2,3,....., K and j= 1,2,3, ...,t_i. Given a p-dimensional vector of unobservable random effects b_i, y_{ij} are independent with means $E\ (y_{ij}/b_i) = \mu_{ij}\ (b_{ij})$ and variance $var\ (y_{ij}/b_i) = a\ (\square)\ v\ (\mu_{ij}(b_i))$. Here the conditional mean depend on the random effect.

The GLMMs consists of the following parts;

1. The linear predictor $\square_{ij}(b_i) = x^T_{ij}\beta + z_{ij}b_i$ with y_{ij} independent and from the distribution density of the form;

$$f_i(y_{ij}|b_i, \beta, \Phi) = exp\,[\Phi^{-1}(y_{ij}\theta_{ij} - \psi(\theta_{ij})) + c(y_{ij}, \Phi)] \quad (3.3)$$

2. The random part conditional on random effects bi, y'_{ij}s are independent random variables with conditional densities belonging to exponential dispersion family and have conditional means and variance
3. The link function which is defined as $h\,E(y_{ij}/\mu_{ij}) = x^T_{ij}\beta + z_{ij}b_i$. Here, **h** is called the link function and x_{ij} and z_{ij} are p and q vectors of known covariates. β is a p-dimensional vector of unknown fixed regressor coefficients and $b_i \sim N(0,D)$. Since our response variable is binary, we show this illustration using logistic regression model;

$$logit\ Pr(y_{ij}=1/\mu_{ij}) = \beta_0 + \mu_i + \beta_1 x_{ij} \quad (3.4)$$

This model shows that each individual in our data is exposed to own probability of a normal response (y = 1) which is given by

$$Pr\,(yij = 1/\mu_{ij}) = \frac{\exp(\beta_0 + \mu_i)}{1 + \exp(\beta_0 + \mu_i)} \quad (3.5)$$

The model also indicates that an individual's odds of a normal response are multiples of exp (β_1). The basic principle of the random effects model is that there exists a natural heterogeneity among subjects in a subset of the regression coefficients e.g. in the intercepts. The fundamental assumptions of the random effects model is that b'_is are independent of the explanatory variables.

There are certain assumptions that are made in random effects models:-

1. The conditional distribution of y_{ij} given bi follow a distribution from the exponential family of distributions with pdf $f(y_{ij}/b_i;\beta)$.

2. Given μ_i, the clustered observation $y_{i1}, y_{i2}, \ldots, y_{ni}$, are independent
3. The b_i's are independent and identically distributed.

3.8 Estimation for Generalized Linear Mixed Models

In this study two methods of estimation will be considered namely conditional likelihood and maximum likelihood estimation.

3.8.1 Condition likelihood estimation

The main idea behind conditional likelihood estimation of β is to treat the random effects b_i as nuisance parameters and then estimate β using conditional likelihood of the data given b_i. Treating b as fixed, the likelihood function for β and b can be given as;

$$\prod_{i=1}^{m}\prod_{j=1}^{ni} f(y_{ij}/\beta, b_i) \;\alpha\; \prod_{i=1}^{m}\prod_{j=1}^{ni} exp\,[\theta_{ij} - \psi(\theta_{ij})] \qquad (3.6)$$

Where $\theta_{ij=}\,\theta_{ij}(\beta, b)$. Restricting this to the canonical link functions for simplicity for which $\theta_{ij} = x^T_{ij}\beta + d'_{ij}b_i$, the likelihood becomes;

$$exp\beta' \sum_{i,j} x_{ij}\, y_{ij} + \sum_{i} b'_i \sum_{j} d_{ij} y_{ij} - \sum_{i,j} \psi(\theta_{ij}) \qquad (3.7)$$

3.8.2 Maximum Likelihood estimation

In maximum likelihood estimation, b_i is treated as a sample of independent unobservable variables from a random effects distribution. This assumption suggests that by understanding the variability of the

overall population, we can learn about an individual's coefficient. Here, the likelihood function for the unknown parameter δ, which is defined to include both β and elements of G, where $b_i \sim i.i.d\, f(\mu_i, G)$ is:

$$L(\delta, y) = \prod_{i=1}^{m} \int \prod_{j=1}^{ni} f(y_{ij}/b_i; \beta)\, f(b_i; G)\, db_i \qquad (3.8)$$

This is simply the marginal distribution of Y obtained by integrating the joint distribution of Y and b with respect to b. The maximum likelihood is found by solving the score function which we obtain by setting the first derivative of the likelihood function above with respect to δ to 0.

The complete data score for β has the form;

$$S_\beta(\delta|y, b) = \sum_{i=1}^{m} \sum_{j=1}^{ni} x_{ij} y_{ij} - \mu_{ij}(bi) = 0 \qquad (3.9)$$

Where $\mu_{ij}(bi) = E(y_{ij}|b_i) = \square^{-1}(x'_{ij} + d'_{ij} b_i)$

These observed data score equations are obtained by taking the expectation of the complete data equations with respect to the conditional distribution of the unobserved random effects given the data. The score function for G is given as;

$$S_G(\delta|y) = \frac{1}{2} D^{-1} \sum^{M} E(b_i b'_i|y_i)\, G^{-1} - \frac{m}{2} G^{-1} = 0 \qquad (3.10)$$

3.9 Logistic regression for binary data

Considering the nature of the response variable in this study, we introduce literature behind logistic regression models as a parametric tool for modeling binary data. Logistic regression models are the most widely used models for categorical response data.

Consider the explanatory variable X of a binary response variable Y and let

$$\pi(x) = prob\ (Y = 1|X = x) = 1 - prob\ (Y = 0|X = x) \tag{3.11}$$

This yield to the logistic regression model;

$$\pi(x) = \frac{\exp(\alpha + \beta x)}{1 + \exp(\alpha + \beta x)} \tag{3.12}$$

In this model the log-odd, which are also called the *logits* has the linear relationship given by;

$$logit[\pi(x)] = log[\frac{\pi(x)}{1 - \pi(x)}] = \alpha + \beta x \tag{3.13}$$

which is the logit link function to the linear predictor. The sign of the β (log odds) determines the slope of the curve i.e. whether π(x) is falling or rising. For quantitative x with $\beta > 0$, the curve of π(x) has the shape of the cumulative distribution function of the logistic distribution, and since the logistic distribution is symmetric, then the π(x) approaches 0 and 1 at the same rate.

Taking exponent of the above equation we get

$$exp\ [Logit[\pi(x)]] = exp\ [\alpha + \beta x] \tag{3.14}$$

This shows that the odds ratios are exponential functions of x. Therefore, the odds increases multiplicatively by e^{β} for every 1-unit increase in x. i.e. e^{β} is an odds ratio, the odds at X = x+1 divided by the odds at X = x.

3.10 Inference in Logistic regression

Wald (1943) showed that the parameter estimators in logistic regression models have (asymptotic) large-sample normal distributions. Thus, inference in logistic regression models can use the Wald, likelihood-ratio methods.

For the model with predictor $Logit[\pi(x)] = \alpha + \beta x$ we test the null hypothesis $H_0 : \beta = 0$ against $H_1 \neq 0$. The wald test uses the log likelihood at β, with the test statistics being $z = \frac{\beta}{SE(\beta)}$. The likelihood ratio test has a χ^2 distribution with 1 degree of freedom and uses twice the difference between the maximized log likelihood at β and at β = 0. One way of checking for the model fitness is by using the likelihood ratio test to compare the fitted model with a more complex model. Another way of checking for model fit is by checking for any way that the model fails. This procedure checks for the model's lack of fit other than model fit.

3.11 Mixed effects models for binary data

In marginal modeling and marginal distributions of clustered responses, the joint dependence structure is treated as a nuisance. There is an alternative approach of using cluster- level terms in the model. These terms are unobserved, taking different values for observations in different clusters. They are treated as varying randomly, hence are called random effects. Random effects models for normal responses are well established and only recently have random effects been used much in models for categorical data. Due to the nature of our outcome variable, we shall narrow this to logistic-normal model. Random

effects models for categorical clustered data in an ordinary linear model, fixed effects refer to parameters that describe a factor's effects and they apply to all categories of interest. Generalized linear models extend ordinary regression by allowing non-normal responses and a link function of the mean, while GLMMs allows random effects as well as fixed effects in the linear predictor.

3.12 The model

If we let y_{it} denote observation t in cluster i, t = 1, . . , T_i. We further let x_it denote a column vector of values of explanatory variables, for fixed effect model parameters β. Again, let μ_i denote the vector of random effect values for cluster i. This is common to all observation in a specific cluster. Let z_{it} donate a column vector of their explanatory variables. Conditional on μ_i, a GLMM resembles an ordinary GLM. The linear predictor for the model is defined as;

$$g(\mu_{it}) = x^T_{it}\beta + z^T\mu_i \qquad (3.15)$$

Where the mean $\mu_{it} = E(Y_{it}|\mu_i)$ and g (.) is the link function. It's further assumed that $\mu_i \sim N(0, \sum)$. We shall introduce here the inter-class and the intra-class correlation in mixed effects model. The intra-class correlation is given by:

$$\rho = \frac{\tau_2}{\tau_2 + \sigma_2} \qquad (3.16)$$

Where τ^2 is the within group variation, and σ^2 is the overall variation, i.e. residual error. The variability of among μ_i induces a non-negative correlation for the marginal distribution that is averaged over the subjects. Observations within the same cluster i share the same mean μ_i. Random effects also enter into our model as any other explanatory variables. .The purpose of including random effects in a model include among others;

- They at times will represent the heterogeneity in the data that is caused by not observing certain predictors. Therefore, random effects model the unobserved predictors by reflecting these terms that would have been in the model.
- They provide a way of explaining the over-dispersion in basic models that do not have these effects.
- They reflect terms that would otherwise be in the fixed effects part of the model if certain predictors would be included in the model.
- They represent random measurement errors in the independent variables.

3.13 Binary responses

The univariate random effect model is of the form;

$$logit\ (\ P\ [Y_{it} = 1/\mu i]) = x^{T}_{it}\,\beta + \mu_{it} \qquad (3.17)$$

Where μ_i independent ~ N $(0, \sigma^2)$ variates. This model is a special case of a generalized linear mixed model and g (.) is the usual logit link function. Let Φ denote the cumulative density function (cdf) that is the inverse link function. Then, for any s $\neq$ t,

$$cov\ (Y_{is}, Y_{it}) = E\ [\ cov\ (Y_{is}, Y_{it}|\mu_i \quad)] + cov[E(Y_{is}|\mu_i),\ E(Yi_t|\mu_i)] = 0 + cov\ [\Phi(x^{T}_{is}\beta + \mu_i),\ \Phi(x^{T}_{it}\beta + \mu_i)]. \qquad (3.18)$$

You shall notice that both $\Phi\ (x^{T}_{i}\,s\beta + \mu_i)$ and $\Phi\ (x^{T}_{i}\,t\beta + \mu_i)$ are monotonically increasing with μ_i, therefore are non-negatively correlated. At each t, the predictor variable j pdf of x is interchangeable for clustered data, a factor that is common also with longitudinal data, where observations in close together time wise are likely to be more correlated than observations that are further apart. In estimation, the interpretation is a around the fixed effects, with the random effects used for example, σ the estimate of

the standard deviation of the random intercept may be used to predict the population's degree of heterogeneity.

$\sigma = 0$- The model simplifies to a logistics regression model, with all observations independent of each other. Recall the log odds ratio given by;

$$logit\,[P\,(Y_{it} = 1|u_i)] - logit[P(Y_{hs} = 1|\mu_h)] = (x_{it} - x_{hs})^T\beta + (\mu_i - \mu_h) \quad (3.19)$$

recall that $(\mu_i - \mu_h) \sim N(0, 2\sigma)$. Thus, $100(1-\alpha)\%$ of the log odds fall with the following range;

$$(x_it - x_hs)^T\beta \pm z\frac{\alpha\ \sqrt{(2\,\sigma\ )}}{2} \quad (3.20)$$

$\sigma > 0$ – the log-odds ratio of two observations in same cluster

3.14 Introducing multilevel models

Most data sets that are collected in human surveys tend to be inherently correlated through clustered nature due to the design of the surveys. The denomination of clusters basically refers to a two level hierarchy, where some basic units of measurement are grouped into clusters. A good example includes Litter effects in animal study and subject effects in repeated measurements. In most complex surveys, this procedure is more common in the process of generating a more parsimonious sample, which is not affected by sampling errors, hence resulting in systematic samples or cluster samples, in place of sample random samples. In analyzing this kind of data whose sample was selected through multistage sampling, then we need to consider using statistical procedure that takes into account the correlation between units that are in the same cluster. This leads us to the use of multi-level modeling techniques. Multi-level models are categorized into two parts; Continuous and discrete multi-level models. Due to the nature of

the response variable (Binary), the discussion in this section will be based on the discrete multi-level models, with special emphasis on those that can be used on binary data.

3.15 Multilevel models for continuous data

Consider a sample with K clusters, with J_k household within the k-th cluster (k=1,2,3,…,K) and members in the j-th household in the k-th cluster (j=1,2,3,….,J_k). Again let's assume y_{ijk} is the values assumed by the response variable associated to the i-th members of the j-th household in cluster k. Then;

$$y_{ijk} = x_{ijk}\beta + z^{(3)}_{ijk}\upsilon_k + z^{(2)}_{ijk}\mu_{jk} + z^{(1)}_{ijk}\varepsilon_{ijk} \qquad (3.21)$$

Where x_{ijk} and z'_{ijk} s are fixed covariates and β is a fixed vector of parameters, and υ_k μ_{jk} and ε_{ijk} are mutually independent and normally distributed random variables. The $\upsilon'_k s$ and the μ'_{jk} s are unobserved/latent variables that are used to model variation in data that is attributed to the clustering effect at different levels depending on the survey design.

When $z^{(3)}_{ijk} = z^{(2)}_{ijk} = 1$, the above model reduces to a simple random intercept model. When $z^{(1)}_{ijk} = 1$, then this model only includes a simple residual error term. However, the possibility of adding extra covariates permits the representation of complex variation at level 1, including subgroup variability (heteroscedasticity). Parameter estimation can easily be done by maximum likelihood estimation procedures that maximize the likehood functions.

3.16 Multilevel models for discrete data

As stated, the discussion in this section concentrates on binary data multilevel models due to the nature of the response variable. If we assume a random variable as defined in the above section, then here we shall consider the model below;

$$logit[(\pi_{ijk})] = x_{ijk}\beta + z^{(3)}_{ijk}\upsilon_k + z^{(2)}_{ijk}\mu_{jk} \quad (3.22)$$

Where $\pi_{ijk} = P[yijk = 1|\upsilon_k, \mu_{jk}]$. For this discussion we shall assume that y_{ijk} ~Bernoulli (π_{ijk}), and therefore the above model can as well be written as;

$$Y_{ijk} = \pi_{ijk} + z^{(1)}_{ijk}\varepsilon_{ijk} \quad (3.23)$$

With $z^{(1)}_{ijk} = \pi_{ijk}(1- \pi_{ijk})$, and π_{ijk} ~(0,1).

For inference and estimation procedures, we can maximize the marginal likelihood obtained after integrating the random effects. But due to computational bulkiness of marginal likelihood and the resulting intractable expression, one has to use numerical integration procedures such as Gaussian quadrate (zeger and karim 1991) and Markov chain Monte Carlo techniques. But again, these procedures can be computationally difficult and therefore other approximate procedures have been suggested among them Breslows penalized quasi likelihood (PQL) and marginal quasi likelihood (MQL).

The model above can also be written as;

$$logit\,[\,Pro(Y_{ijk} = 1|\mu_{ij})] = \beta_0 + \mu_{ij} + x_{ijk}\beta \quad (3.24)$$

for simplicity purpose, we assume that $\gamma_{ij} = \beta_0 + \mu_{ij}$ and further assume that x_{ijk} does not include n intercept term. Then, the joint likelihood functions for β and γ is proportional to;

$$\prod_{i=1}^{m}\prod_{j=1}^{ni} exp\,[\,\gamma_{ij}\sum_{k=1}^{K} y_{ijk} + (\sum_{k=1}^{K} y_{ijk}x_{ijk})\beta - \sum_{k=1}^{K}\log 1 + exp(\gamma_{ij} + x'_{ijk}\beta)] \quad (3.25)$$

The conditional likelihood of β given the sufficient statistics for the γ_{ij} is of the form given by;

$$\prod_{i=1}^{m} \prod_{j=1}^{ni} \frac{\exp(\sum_{k=1}^{K} y_{ijk} x_{ijk} \beta)}{\sum_{Rij} \exp(\sum_{l=1}^{yij} y_{ij} x'_{ijl} \beta)} \tag{3.26}$$

Where R_{ij} contains all the $(n_{ij}C_{ij})$ ways of choosing y_{ij} positive responses out of n_{ij} correlated observations.

CHAPTER FOUR

APPLICATION OF GLMMS IN MODELING MORBIDITY EPISODES AND ANALYSIS OUTPUT

Statistical tools for Microsoft excel, SPSS and R were used for data input and analysis. Some of the explanatory variables were categorized before starting the analysis into two or more categories to make the analysis and interpretations more meaningful. Exploratory data analysis is done using SPSS and R statistical software, data is then fed into models for further analysis.

4.1 Variable descriptions

1. Diseased:- This is a binary variable defined as 1 if an environmental health related disease occurred or 0 if it didn't occur to an individual
2. Gender:- sex of an individual- coded as 1= Male, 0=Female thus it's a categorical variable with 2 levels
3. Highest education attained:- it's a categorical variable with four levels coded 0=None, 1=primary, 2=secondary and 4=tertiary
4. Current working status:- A categorical variable coded 1=working and 0=Not working.
5. Area of Residence :- A categorical variable with 1=Rural and 0= Urban
6. Main source of drinking water :- is a categorical variable coded 1-safe drinking water and 0= unsafe drinking water
7. Human waste disposal:- A binary variable defined as 1 if one use hygienic human waste disposal means or 0 if not
8. Housing condition :- is a binary variable coded 1 if has good housing condition and 0 if has poor housing condition
9. Clust:- clustering variable

4.2 Modeling individual morbidity using Generalized Linear Mixed Model

We fit a GLMM effect model to the individual morbidity data described above. The dependent variable is "diseased", as a measure of whether an individual experienced environmental health related disease.

4.3 The individual model

The generalized linear mixed effects model with logit link is defined as below:

$$logit[Pr(y_{ij} = 1|\mu_i)] = \beta_0 + \mu_i + \beta_{ixij} \quad (4.1)$$

the model takes the form;

$$\text{logit}[(\text{Prob}(\text{disease } d_{ij}) = 1|\mu_i)] = \beta_0 + \mu_i + \beta_1(\text{gender})_{ij} + \beta_2(\text{education})_{ij} + \ldots\ldots\ldots + \beta_7(\text{housing})_{ij} + b_0(\text{clust}). \quad (4.2)$$

We begin by showing the distribution of different dependent variables. The table below shows all the variables that were fitted in the model.

4.4 Exploratory data analysis

In this section we seek to show the distribution of the dependent variable compared to some selected covariates.

Table 4.4: Summary statistics (Categorical variables)

Variable	Category	Descriptive	Percentage
Gender	Male	32,918	49.3
	Female	33,807	50.7

Area of residence	Rural	47,126	70.9
	Urban	19,351	29.1
Working status	Working	14,895	66.9
	Not working	7,374	33.1
Source of drinking water	protected source	32,870	50.1
	unprotected source	32,732	49.9
Human waste disposal	hygienic waste disposal	31,158	47.5
	unhygienic waste disposal	34,495	52.5
Highest Education	None	28,731	61.1
	Primary	9,920	21.1
	Secondary	4,896	10.4
	Tertiary	3,505	7.4
Housing condition	good housing condition	38,788	59.3
	poor housing condition	26,670	40.7

Table 4.5: Cross-tab of all covariates against the dependent variable "diseased"

Variable	Level	Non diseased	diseased	Total	Cramer's V
gender	Male	50.3	45.6	49.3	0.037
	Female	49.7	54.4	50.7	
Area of residence	Rural	71.1	70.1	70.9	0.009
	Urban	28.9	29.9	29.1	
Working status	Working	66.4	69.2	66.9	0.023
	Not working	33.6	30.8	33.1	
main source water	protected source	49.8	51.2	50.1	0.011
	unprotected source	50.2	48.8	49.9	
human waste disposal	hygienic waste disposal	46.9	49.5	47.5	0.02
	unhygienic waste disposal	53.1	50.5	52.5	
highest education		60.4	64.2	61.1	0.033
	None	21.4	19.5	21.1	
	Primary	10.7	8.9	10.4	
	Secondary	7.5	7.4	7.4	
	Tertiary				
housing condition		59.1	59.8	59.3	0.005
	good housing				

	condition poor housing condition	40.9	40.2	40.7	

We fit a GLMEM using the lmer command in R which contains functions for estimation of multilevel or hierarchical regression models. β represents the coefficients of fixed effects while b's represent the coefficients of the random part.

A generalized linear mixed effect model for all explanatory variables in R produced the model in the table 4.7 below.

Table 4.8 shows the fitted GLM with outcome "diseased". This model uses a logit link to estimate the factors that drive morbidity incidences. We use this model to compare the results from the GLMEM reported previously.

Table 4.6: Model 1 Null linear mixed model by REML

AIC	BIC	LogLink	Deviance	REML dev
63774	63792	-31885	63857	63770

Random effects

Groups	Name	Variance	Std.Dev
Clusters	Intercept	0.011986	0.10948
Residual		0.147679	0.38429

Fixed effects:

	Estimate	Std.Error	z value	Pr(>|z|)
Intercept	1.53199	0.02271	67.45	<2e-16 ***

The above model is an empty model i.e model fitted without including the explanatory variables. The variance component corresponding to the random intercept is 0.011986.

The two variance components can be used to partition the variance across levels. The interclass correlation coefficient is equal to;

$\rho = \frac{0.011986}{0.011986 + 0.147679}$ =0.075 meaning that roughly 0.08% of the variance is attributed to the cluster-level. The strength of the intra-cluster correlation determines how observations within a given cluster are likely to be similar to each other. Thus, a higher intra-cluster correlation gives a more pronounced "clustering effect."

To explain some of the cluster-level variance, we incorporate the explanatory variables in the empty model. The table below shows the GLMM for the random intercept and fixed predictors in individual level using REML.

Table 4.7 Model 2: GLMM for the random intercept and fixed predictors using REML

AIC	BIC	Loglink	deviance	REML dev
3946	4023	-1961	3855	3922
Random effects				
Groups	Name	Variance	Std.Dev	
Clusters	Intercept	0.0077387	0.08797	
Residual		0.1393540	0.37330	
Fixed effects				
	Estimates	Std.Error	z value	Pr(>|z|)
(intercept)	1.35917	0.13153	10.334	< 2e-16 ***
Male	0.26122	0.08322	3.139	0.00170
Urban	-0.11217	0.13598	-0.825	0.40943
Working	-0.06090	0.09769	-0.623	0.53304
Unprotected water source	0.01772	0.10003	0.177	0.85938
Unhygienic waste disposal	0.10290	0.09925	1.037	0.09984
Primary	-0.01127	0.10086	-0.112	0.91103
Secondary	0.15345	0.13454	1.141	0.25407
Tertiary	0.04185	0.12827	0.326	0.74420
Poor housing condition	0.23273	0.10640	2.187	0.02872

The variance component corresponding to the random intercept has decreases to 0.0077387, indicating that the inclusion of the explanatory variables has accounted for the some of the unexplained variance. Comparing both the AIC and BIC statistics in both models above, it is clear that the model 2 is preferable to the model 1since it gives smaller values of AIC and BIC.

From the GLMM model above; gender, human waste disposal and housing condition are significant in predicting the probability of an individual getting an environmental health related disease. However, area of residence, education and working condition and main source of water are insignificant.

The GLMM model is of the form

$$\text{logit}\ [(\text{prob}(\text{disease}\ d_{ij}) = 1/\mu_i] = \beta_0 + \mu_i + \beta_1(\text{gender})_{ij} + \beta_2(\text{human waste disposal})_{ij} + \beta_3(\text{housing condition})_{ij} \quad (4.3)$$

The GLMM outputs above indicates that with group of the female as the reference group; then the log of odds of getting an environmental health related disease increases by 0.0017.

Holding other variables constant; an individual living in poor housing condition is about 3% more likely to have the disease compared to an individual living in a good housing condition. Also the odds of getting an environmental health related disease is exp (0.09984) = 1.10499 times for unhygienic waste disposal compared to hygienic means of human waste disposal.

Table 4.8: A generalized linear model for "diseased"

AIC	4002.792			
	Estimate	Std. Error	z value	p-value
(intercept)	1.232434	0.11169	11.034	2.00E-16
Male	0.24782	0.080393	3.083	0.002052
Urban	-0.108088	0.104391	-1.035	0.300476
Working	-0.097075	0.09077	-1.069	0.28486
unprotected source	0.041063	0.083227	0.493	0.001744
unhygienic waste disposal	0.145195	0.087092	1.667	0.095486
poor housing condition	0.323525	0.089386	3.619	0.000295
Primary	0.002356	0.096739	0.024	0.980572
Secondary	0.182476	0.12824	1.423	0.154758
Tertiary	0.056151	0.121077	0.464	0.64282

The Akaike Information Criteria (AIC) for GLM model was 4002.792 which is a measure of goodness of fit that takes the number of fitted parameters into account. This value is larger as compared to AIC in the GLMM model. Thus GLMM model is preferable to GLM in modeling clustered data.

From the GLM model above;, gender, human waste disposal, housing condition and main source of drinking water are significant in predicting the probability of an individual getting an environmental health related disease. However, area of residence, education and working condition are insignificant.

Hence the GLM model would be

$$ln \frac{P(y=1|x)}{1-P(y=1|x)} = \beta_0 + \beta_1(\text{gender}) + \beta_2(\text{housing condition}) + \beta_3(\text{main source of water}) + \beta_4(\text{human waste disposal}) \quad (4.4)$$

The GLM outputs above indicates that with group of the female as the reference group; then the log of odds of getting an environmental health related disease increases by 0.24782. For the main source of water variable, the odds of getting an environmental health related disease is exp (0.041063) = 1.0419 times for unprotected main source of water compared to protected source of water. Holding other variables constant; an individual living in poor housing condition is about 38% more likely to have the disease compared to an individual living in a good housing condition. Also the odds of getting an environmental health related disease is exp (0.145195) = 1.1563 times for unhygienic waste disposal compared to hygienic means of human waste disposal.

CHAPTER 5

CONCLUSSION, RECOMMENDATINS AND SUGGESTIONS FOR FURTHER STUDIES

5.1 Introduction

This chapter provides conclusion, recommendations and suggestions for further studies.

5.2 Conclusion

This study was set to determine factors that are associated with the probability of an individual in a population experiencing an environmental health related disease in Kenya. It was also set to develop a statistical model that describes the influence of these factors while accounting for inter-class correlation in the data. The study found that individual morbidity is associated with some social, economic and demographic factors in the country. The study applied both GLM and GLMM models to model household data that was collected in 2005/6 to investigate factors associated with environmental health related diseases. Further, the study applied Akaike Information Criteria (AIC) to determine the preferable model in modeling clustered data.

From the analysis, it was found that, the severity of environmental health related disease is likely to increase with gender whereby a female individual is likely to get a disease than a male individual. This outcome supports the idea that gender-specific differences in morbidity and mortality may be explained by genetic factors and by their differential response to the environment.

People living in poor housing conditions were found to be more likely to get a disease than those from good housing condition. Main source of drinking water was also significant in explaining individual morbidity in Kenya with an individual using unprotected main source of water found more likely to get a disease than an individual using protected main source of water.

Means of human waste disposal was another factor found affecting the disease outcome whereby an individual using unhygienic waste disposal was more likely to have an environmental health related disease than the one using hygienic means.

However, the study found that area of residence; working condition and education level do not affect the diseased outcome.

On the statistical model that account for inter-class correlation in the data, it was found that the value of AIC in GLM model was larger compared to AIC value in GLMM model. According to Akaike's theory, the most accurate model has the smallest AIC hence; for this study, it could conclude that GLMM model is more preferable to GLM in modeling clustered household data.

5.3 Recommendations

Efforts to address the plight of the environmental health related disease should be more focused to individuals living in poor conditions and should not only be focus in offering facilities but also economic empowerment.

5.4 Suggestions for Further Studies

This study can be extended to incorporate income level of individuals. Individuals with low level of income are believed to be more likely to experience environmental health related diseases than individuals with higher levels of income.

Further studies should also be carried out to focus on mapping the areas which are mostly affected in the country and developing an effective model to address the issue.

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APPENDIX

R Syntax Commands used

GLMM Commands

```
mydata=read.csv(file.choose())

attach(mydata)

mydata

library(lme4)

install.packages("lme4")

#null-model

lmer(y ~ 1 + (1 | clusters), data=mydata)

#random intercept, fixed predictor in individual levelusing REML

lmer(y ~ x1+x2+x4+x5+x6+x7+x8 + (1 | clusters), data=mydata)

#random intercept, fixed predictor in individual levelusing ML

lmer(y ~ x1+x2+x4+x5+x6+x7+x8 + (1 | clusters), data=mydata, method="ML")
```

GLM model Commands

```
mydata=read.csv(file.choose())
attach(mydata)
mydata library(mlogit)
mydata$y<-as.factor(mydata$y)
mldata<-mlogit.data(mydata, varying=NULL, choice="y", shape="wide")
mlogit.model<-mlogit(y~x1+x2+x3+x4+x5+x6+x7+x8, data=mydata, reflevel="diseased")
summary (mlogit.model)

mylogit<-glm(y~x1+x2+x4+x5+x6+x8+x7, data=mydata, family=binomial)
Summary (mylogit)
AIC (mylogit)
```